

1) Evaluate the iterated integral.

a)  $\int_0^1 \int_0^{x^2} (x+2y) dy dx$

b)  $\int_0^1 \int_y^{e^y} \sqrt{x} dy dx$

c)  $\int_0^{\pi/2} \int_0^{\cos y} e^{\sin y} dx dy$

2) Evaluate the double integral.

a)  $\iint_D x \cos y dA$ ,  $D$  is bounded by  $y=0$ ,  $y=x^2$ ,  $x=1$

b)  $\iint_D y^3 dA$ ,  $D$  is the triangular region with vertices  $(0,2)$ ,  $(1,1)$ ,  $(3,2)$

c)  $\iint_D (2x-y) dA$ ,  $D$  is bounded by the circle with center at the origin and radius 2.

3) Find the volume of the given solid:

- a) Enclosed by the paraboloid  $z = x^2 + 3y^2$  and the planes  $x = 0$ ,  $y = 1$ ,  $y = x$ ,  $z = 0$ .
- b) Bounded by the cylinder  $x^2 + y^2 = 1$  and the planes  $y = z$ ,  $x = 0$ ,  $z = 0$  in the first octant.

4) Find the volume of the solid by subtracting two volumes. The solid enclosed by the parabolic cylinders  $y = 1 - x^2$ ,  $y = x^2 - 1$  and the planes  $x + y + z = 2$ ,  $2x + 2y - z + 10 = 0$ .

5) Evaluate the integral by reversing the order of integration:

a)  $\int_0^3 \int_{y^2}^9 y \cos(x^2) dx dy$

b)  $\int_0^1 \int_{\arcsin y}^{\pi/2} \cos x \sqrt{1 + \cos^2 x} dx dy$

6) Find the average value of  $f(x, y) = e^{x+y}$  over the region  $R$  represented by the triangle with vertices  $(0,0), (0,1), (1,1)$ .